

Assignment for Academic Year 2025-2026 (Session Beginning January 2026)

CLASS: BA-1<sup>st</sup> Year

Course Name: Differential Equations

Course Code: MATH102TH

**ASSIGNMENT-1**

Attempt any **TWO** of the following questions:

- Ques 1.** Solve the differential equation  $(x^2 + y^2 - a^2)x dx + (x^2 - y^2 - b^2)y dy = 0$ .
- Ques 2.** Show that  $\frac{1}{x^2}$  is an integrating factor of the equation  $y dx - x dy = 0$ . Also solve it.
- Ques 3.** (a) Show that the functions  $e^{ax}$  and  $e^{bx}$  are L.I. unless  $a = b$ .  
(b) Show that the functions  $e^{2x} \sin 3x$ ,  $e^{2x} \cos 3x$ ,  $e^{2x}(2 \sin 3x + 5 \cos 3x)$  are linearly dependent.
- Ques 4.** Find the necessary and sufficient condition that the equation  $M dx + N dy = 0$  (where  $M$  and  $N$ ) are functions of  $x$  and  $y$  with the condition that  $M, N, \frac{\partial M}{\partial y}, \frac{\partial N}{\partial x}$  are continuous functions of  $x$  and  $y$ ) may be exact.

**ASSIGNMENT-2**

Attempt any **TWO** of the following questions:

- Ques 1.** Solve  $\frac{d^2y}{dx^2} - 7\frac{dy}{dx} + 6y = e^{2x}$  given that  $y = 0$  when  $x = 0$ .
- Ques 2.** Solve  $\frac{d^2y}{dx^2} - y = \frac{2}{1+e^x}$  by the method of variation of parameters.
- Ques 3.** Solve  $y = 3px + 4p^3$
- Ques 4.** Solve  $\frac{d^3y}{dx^3} + \frac{d^2y}{dx^2} - \frac{dy}{dx} - y = \sin 2x$

**ASSIGNMENT-3**

Attempt any **TWO** of the following questions:

- Ques 1.** Find the complete solution of  $2z + p^2 + qy + 2y^2 = 0$
- Ques 2.** Solve  $s = 2x + 2y$
- Ques 3.** Classify and reduce to canonical form  $\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial y^2} = 0$ , Find its solution also.
- Ques 4.** Find the general solution of the following Lagrange's linear equation  $(y + z)p + (z + x)q = x + y$ .